

# Rumor Spreading Modeling: Profusion versus Scarcity

*Martine Collard\**, *Philippe Collard\*\**, *Laurent Brison\*\*\**, *Erick Stattner\**

\* LAMIA Laboratory, University of the French West Indies, France

\*\* I3S Laboratory, University of Nice-Sophia Antipolis, France

\*\*\* Lab-STIC Laboratory, Telecom Bretagne, France

DYNO Workshop - ASONAM 2015



# Dissemination of rumors

Information: news, opinion, disease, virus, **rumors**

- How to model the propagation?
- Analogies among different kinds of information
- Particular emphasis on epidemical models in the literature
- Compartment models, Meta-population models, Network-based models
- Formal representation, Agent based simulations and Real data analysis
- **Word of mouth** rumors and Online rumors

# Outline

- 1 Context
- 2 Spatial model of rumor spreading
- 3 Simulation
- 4 Conclusion

# Outline

- 1 Context
- 2 Spatial model of rumor spreading
- 3 Simulation
- 4 Conclusion

# Context

## Compartment models

- Rumors studied for years originally in economics, psychology and social sciences (Knapp 1944, Rosnow & Fine 1976)
- Epidemiological mathematics and stochastic solutions (Kermack & Kendrick 1927)
- Agent-based and data driven simulations
- SIR: Three compartments (**S**usceptible **I**nfected **R**ecovered)



# Context

## Daley Kendall model

Rumor propagation is highly specific

- *Currently circulating story or report of uncertain or doubtful truth* (Oxford dictionary)
- A kind of contagion process
- Multi-dimensional process driven mainly by socio-psychological elements
- DK Model (Daley & Kendall, 2006): Three compartments (*Ignorant, Spreader and Stifler*)



- DK: principle of novelty  
for an individual likely to tell the story, there is a *reluctance to tell stale news*

# Context

## SIR and DK Assumptions

### Assumptions in SIR and DK

- The population is fully mixed
- Individuals with whom a susceptible individual has contacts are chosen at random into the whole population
- All individuals have approximately the same number of contacts in the same period of time
- The transition from one state to another one relies on a same probability for every individual

# Context

## Rumor specific properties

On the global scale

- **Longness** since it takes a relative long time for Spreaders to tell the story so that the rumor starts (Zhao al. 2012)
- **Slowness** since the propagation starts slowly and the information spreads in a short time (Kawachi al. 2008)
- **Incompleteness** since the infection does not reach the whole population (Daley and Kendall 2006)
- **Sparseness** since individual neighborhoods are not densely populated by Spreaders (Kawachi al. 2008)

Rosnow and Fine (1976) identified the feature of **scarcity** as a key dimension for rumor spreading: *Rumours arise when information is scarce*



# Context

## This work

- Word of mouth rumors very difficult to follow, they do not generate data as online rumors that propagate on social media
- Investigation of the **profusion/scarcity** property of the rumor
- New perspective on the context of individuals likely to tell the story themselves once they know it
- A spatiotemporal model of rumor spreading
- What is the most realistic between the two antagonistic properties profusion and scarcity to disseminate a rumor?

# Outline

- 1 Context
- 2 Spatial model of rumor spreading**
- 3 Simulation
- 4 Conclusion

# Spatial model of rumor spreading

## ODS Model

- A rumor is transmitted by word of mouth from individuals to individuals
- Spatiality, contact, social environment and psychological context are cornerstones of the phenomena
- **ODS model** relies on physical contact and mobility
- Each individual has a location in a world represented by a grid composed of cells
- His/Her neighborhood is composed by the others around him/her
- Individuals are mobile, they create new social contacts when they move
- The diffusion is relying on the induced social network and on individual spreading behaviour
- With spatiality, mobility, dynamicity and socio-psychological aspect, the goal is to better fit the framework to reality

# ODS model

## Compartments

- **Open-minded** agents are the individuals who have not yet heard the rumor, and, consequently, are susceptible to becoming informed
- **Disseminators** are active individuals that are spreading the rumor
- **Stiflers** are individuals that have got the rumor but are no longer spreading it

The total population size  $N = O + D + S$

# Spatial model of rumor spreading

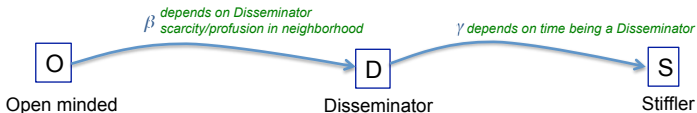
ODS vs SIR and DK

- The aim is to model the spreading of a rumor, thus with the spatial dimension
- Contacts between individuals are not chosen at random and they occur between neighbors only
- Agents are moving, at each time step, the number of contacts for an individual is not a constant
- The probability that a D-individual transmits the information to an O-individual upon contact depends on each individual and varies over time. It is referred as  $\beta_k^{OD}(t)$

# ODS Model

## Transitions

- The potential receiver, and not the transmitter, decides whether or not he will become itself a transmitter:  
Crucial difference with infectious disease spreading
- An **O**-individual  $a_k$  becomes himself a **D**-individual according to a function of the rate  $r_k^D$  of D-individuals in his neighborhood.
- Two alternative solutions:
  - 1  $ODS_p$  driven by the *profusion* of information
  - 2  $ODS_s$  driven by the *scarcity* of information according to the number of D-individuals in the vicinity



# Outline

- 1 Context
- 2 Spatial model of rumor spreading
- 3 Simulation**
- 4 Conclusion

# Simulation

## ODS Algorithm

1.  $t \leftarrow 0$
2. Initialize the parameter  $DPeriod$   $\{\gamma \leftarrow \frac{1}{DPeriod}\}$
3. Initialize the population size to  $N$
4. Create  $N$  agents  
    {each agent have a *state* variable in  $\{O, D, S\}$ }
5. Place at random the  $N$  agents on the grid  
    {each agent have a *position* in the 2-D space}  
    {each agent have a *heading* which indicates the direction he is facing}
6. Set all the agents  $O$  except one which is  $D$
7. **while**  $\exists$  one  $D$  agent **do**
8.     Call OtoD
9.     Call DtoS
10.    Call walk {ask all agents to move}
11.     $t \leftarrow t + 1$
12. **end while**



# Simulation

## Transmissibility potential

To report if the invasion will succeed or not:

Reproductive ratio  $R_0 = \frac{\beta \times N}{\gamma}$  that is the number of secondary infections that result from a single Infected individual in a fully Susceptible population

$ODS_s$  results are consistent with the *longness* feature

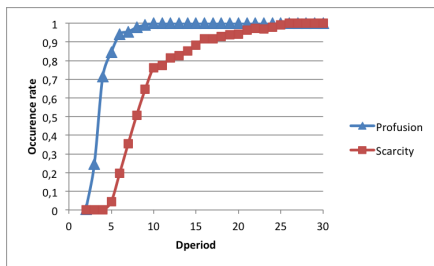


Figure : Probability for a rumor to occur plotted against *Dperiod*

# ODS model

## Rumor curve

Rumor curve as an epidemic curve:  $ODS_s$  process is starting much slower and has a smaller amplitude than in case of profusion

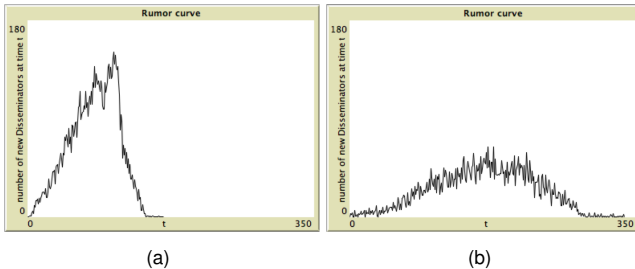


Figure : Rumor curve ( $Dperiod = 10$ ), profusion (a) scarcity (b)

# ODS model

Number of individuals in each compartment

At the end of the process, with  $ODS_s$  there remain individuals that are not Stiflers

Consistent with the incompleteness feature

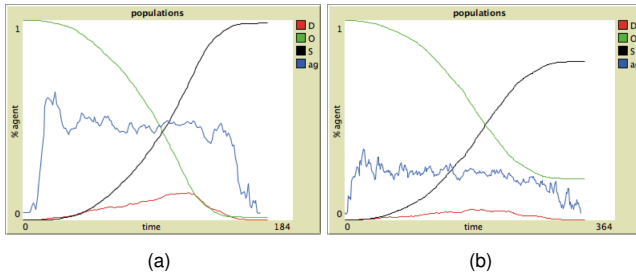


Figure : Proportion of individuals in each compartment as a function of time ( $D_{period} = 10$ ), profusion (a), scarcity (b)

# ODS model

## Spatial distribution of compartments

### D-aggregation index

$$ag_D(t) = \frac{1}{|D|} \sum_{k \in D} p_k^D(t)$$

where  $p_k^D(t)$  can be interpreted as the profusion of disseminators around an individual  $a_k$ .

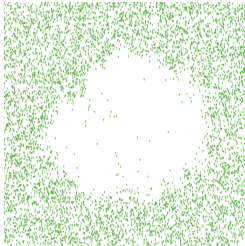
Low values of  $ag_D(t)$  means that D-individuals will be spread over the world  
High values correspond to configurations with more homogeneous patterns of D-individuals

D-aggregation index evolution: blue curve

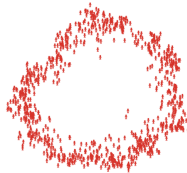
# ODS model

## Spatial distribution of compartments

### Profusion



(a)  $t = 70$



(b)  $t = 70$



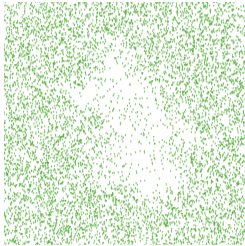
(c)  $t = 70$

Figure : Spatial distribution of compartments ( $D_{period} = 10$ ) with profusion and O-persons (a), D-persons (b), S-persons (c)

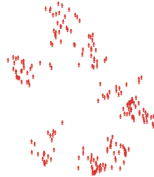
# ODS model

## Spatial distribution of compartments

### Scarcity



(a)  $t = 120$



(b)  $t = 120$



(c)  $t = 120$

Figure : Spatial distribution of compartments ( $D_{period} = 10$ ) with scarcity and O-persons (a), D-persons (b), S-persons (c)

### Consistent with sparseness

# Conclusion

- We have proposed a model of rumor diffusion that integrates the local context of individuals making the phenomenon
- Agent-based simulations have shown that scarcity induces characteristic features of a rumor identified as longness, slowness, incompleteness and sparseness
- Next step will consider an explicit social network like a scale free network